

# Magnetic Resonance Imaging

## Lecture 3; Section 1: Encoding spatial information: 2

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## Section 1

# Encoding spatial information into net magnetisation

## Spatial encoding and field gradients

Gradient pulse causes Larmor frequency to become a function of position

So, the phase of the nuclear precession will become a function of position over the period of a gradient pulse

Exploit these features to:

- Encode  $x$  position into  $k_x$  via “frequency encoding”
- Encode  $y$  position into  $k_y$  via “phase encoding”

Remember, gradient pulses  $G_i$  are such that:

$$B_z(x, y, z, t) = B_0 + xG_x(t) + yG_y(t) + zG_z(t)$$

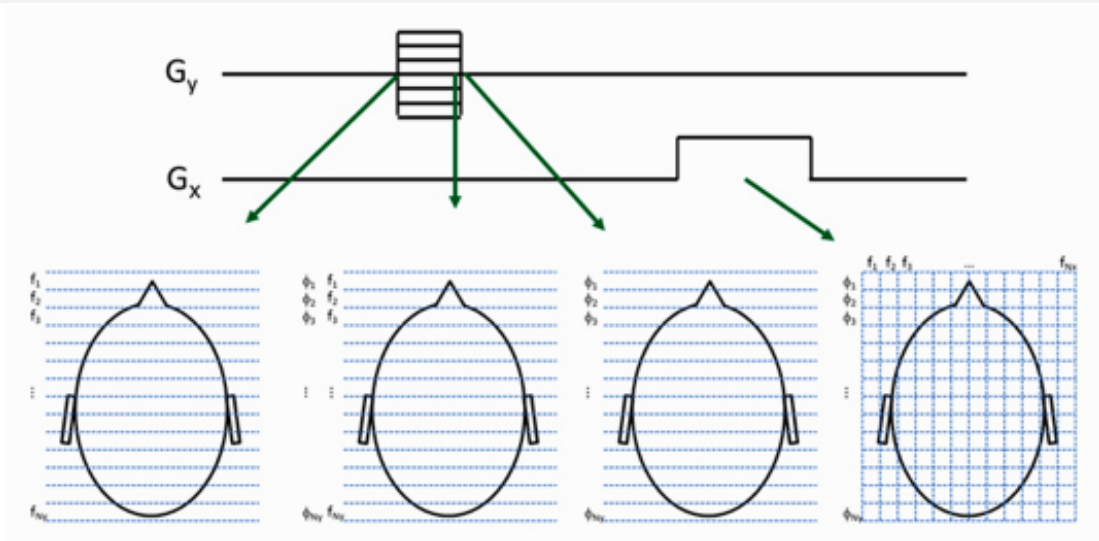
$G_x = \frac{\partial B_z}{\partial x}$ ; i.e. a magnetic-field gradient in  $x$  direction

**magnetic field  $xG_x$  is in the  $\hat{k}$  direction**

$G_y = \frac{\partial B_z}{\partial y}$ ; i.e. a magnetic-field gradient in  $y$  direction

**magnetic field  $yG_y$  is in the  $\hat{k}$  direction**

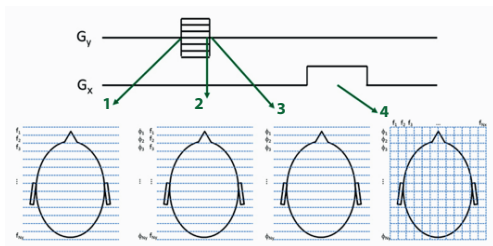
# Conversion of field gradient into $k$ space



# Conversion of field gradient into $k$ space

Example:

phase encode  $y$ ,  
frequency encode  $x$

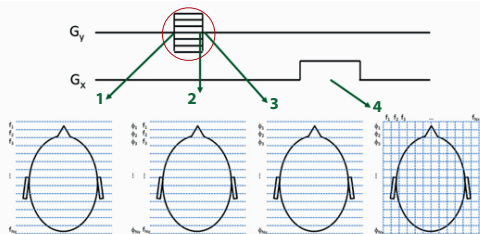


- ① At start of phase encoding-pulse, spins are in phase.  $G_y$  causes Larmor frequency to be function of  $y$ :  $\nu = f(y)$
- ② At end of phase encoding pulse, phase of precession,  $\phi$ , has become a function of  $y$ , i.e.  $\phi \rightarrow \phi(y)$
- ③ As time passes, phase dependence on  $y$  is preserved, i.e.  $\phi = \phi(y)$
- ④ Gradient pulse  $G_x$  causes Larmor frequency to become a function of  $x$ . Result is that  $y$ -position information is encoded in  $\phi = \phi(y)$  and  $x$ -position information is encoded in  $\nu = f(x)$

# Spatial encoding gradient pulses part of pulse sequence

Example:

phase encode  $y$ ,  
frequency encode  $x$



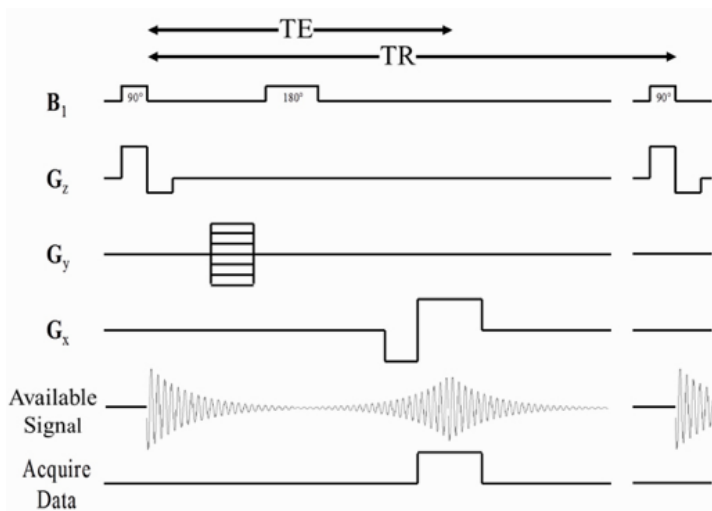
Phase- and frequency-encoding pulses part of a longer pulse sequence that repeats with period TR

At each repeat the amplitude of  $G_y$ , the phase-encoding pulse, has a different amplitude (as indicated on the figure)

For example:

- 1<sup>st</sup> iteration of sequence:  $G_y = 0$ ;
- 2<sup>nd</sup> iteration of sequence:  $G_y = +\eta$ ;
- 3<sup>rd</sup> iteration of sequence:  $G_y = -\eta$ ;
- ...

## Example pulse sequence



Example of spin-echo pulse sequence

Data is acquired at spin-echo time as shown

Combination of phase and frequency encoding pulses and repetition to obtain  $N_y$  data points completes ones transverse slice

## Summary of section 3

*Field gradient* makes Larmor *frequency* a function of position;

*Phase difference as a function of position* develops during application of gradient pulse

Exploit the position dependence of frequency and phase to encode image in  $k$ -space

Pulse sequences designed to optimise contrast within slice for various tissues and types of investigation